

1. Siakan palajari dan diskusikan materi dan soal-soal yang ada pada akhir materi yang terlampir pada FILE.
2. Kemudian jawaban dikirimkan sebelum batas waktu yang sudah ditentukan.

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MID TEST MATEMATIKA TERAPAN

1. a. $f(x) = (2x^2-3)(2x^2-5x+7)$

$$f(x) = 4x^4 - 10x^3 + 14x^2 - 6x^2 + 15x - 21 = 4x^4 - 10x^3 + 8x^2 + 15x - 21$$

$$f'(x) = 16x^3 - 30x^2 + 16x + 15$$

b. $f(x) = \frac{2x-1}{3+x^2}$, misalkan $u: 2x-1$, $u': 2$, $v: 3+x^2$, $v' = 2x$

$$f'(x) = \frac{u'}{v} = \frac{u' \cdot v - v' \cdot u}{v^2}$$

$$f'(x) = \frac{2 \cdot (3+x^2) - 2x \cdot (2x-1)}{(3+x^2)^2} = \frac{6+2x^2-4x^2+2x}{9+6x^2+4x^2} = \frac{-2x^2+2x+6}{x^2+6x^2+9}$$

c. $f(x) = 3(2x-4)^2$

$$f(x) = 3 \cdot (4x^2 - 16x + 16) = 12x^2 - 48x + 48$$

$$f'(x) = 24x - 48$$

d. $f(x) = 5 \cos x - \frac{1}{2}x^2$

$$f'(x) = -5 \sin x - x$$

2. a. $\int \frac{2x+1}{x^2} dx = \int \frac{2}{x} - \frac{1}{x^2} dx = \int 2x^{-1} - x^{-2} dx = 2 \ln|x| + x^{-1} + C = 2 \ln|x| + \frac{1}{x} + C$

b. $\int_0^4 (\sqrt{x} + \frac{1}{\sqrt{x}}) dx = \int_0^4 (x^{\frac{1}{2}} + x^{-\frac{1}{2}}) dx = [\frac{2}{3}x^{\frac{3}{2}} + 2x^{\frac{1}{2}}]_0^4 = [\frac{2}{3} \cdot 4^{\frac{3}{2}} + 2 \cdot 4^{\frac{1}{2}}] - [\frac{2}{3} \cdot 0^{\frac{3}{2}} + 2 \cdot 0^{\frac{1}{2}}]$

$$\int_0^4 (\sqrt{x} + \frac{1}{\sqrt{x}}) dx = (\frac{2}{3} \cdot 8 + 2 \cdot 2) - (0+0) = \frac{16}{3} + 4 = \frac{28}{3} = 9 \frac{1}{3}$$

c. $\int x^2 \cdot \sin x^3 dx$, misalkan $u: x^3$ $\frac{du}{dx} = 3x^2$, $dx = \frac{du}{3x^2}$

$$\int x^2 \cdot \sin x^3 \frac{du}{3x^2} = \frac{1}{3} \int \sin u du = -\frac{1}{3} \cos u + C = -\frac{1}{3} \cos x^3 + C$$

d. $\int 3x(x^2+5)^5 dx$; misalkan $u: x^2+5$, $\frac{du}{dx} = 2x$, $dx = \frac{du}{2x}$

$$\int 3x(u)^5 \frac{du}{2x} = \frac{3}{2} \cdot \frac{1}{6} u^6 + C = \frac{1}{4} (x^2+5)^6 + C$$

3. Diketahui: $u_1: a = 2$, $S_{\infty} = 4$

$$S_{\infty} = \frac{a}{1-r}, \text{ maka } 4 = \frac{2}{1-r} \Rightarrow 4(1-r) = 2 \Rightarrow 4 - 4r = 2 \Rightarrow 4r = 2 \Rightarrow r = \frac{1}{2}$$

4. Diketahui = Deret = $1+4+16+64+\dots$, maka $a=1$, $r=4$

$$S_n = \frac{a(r^n-1)}{r-1} \rightarrow \frac{1(4^n-1)}{4-1} > 1000 \rightarrow \frac{4^n-1}{3} > 1000 \rightarrow 4^n-1 > 3000$$

$$4^n > 3001$$

$$\log 4^n > \log 3001 \rightarrow n \log 4 > \log 3001 \rightarrow n > \frac{\log 3001}{\log 4} = 5,775 \approx 6$$

$$5. f(x) = e^x \cdot \cos(x)$$

$$f(x) : e^x \cdot \cos(x) \rightarrow f(0) = e^0 \cdot \cos(0) = 1 \rightarrow f(c) = e^c \cdot \cos(c)$$

$$f'(x) = e^x \cdot \cos(x) - e^x \cdot \sin(x) \rightarrow f'(0) = e^0 \cdot \cos(0) - e^0 \cdot \sin(0) = 1 \rightarrow f'(c) = e^c \cdot \cos(c) - \sin(c)$$

$$f''(x) : e^x \cdot \cos(x) - e^x \cdot \sin(x) - e^x \cdot \sin(x) - e^x \cdot \cos(x) = -2e^x \cdot \sin(x) \rightarrow f''(0) = -2 \cdot 0 = 0 \rightarrow f''(c) = -2e^c \cdot \sin(c)$$

$$f'''(x) : -2e^x \cdot \sin(x) - 2e^x \cdot \cos(x) \rightarrow f'''(0) = -2e^0 \cdot \sin(0) - 2e^0 \cdot \cos(0) = -2 \rightarrow$$

$$f'''(c) : -2e^c \cdot \sin(c) - 2e^c \cdot \cos(c)$$

$$f^{(4)}(x) = -2e^x \cdot \sin(x) - 2e^x \cdot \cos(x) - 2e^x \cdot \cos(x) + 2e^x \cdot \sin(x) = -4e^x \cdot \cos(x) \rightarrow f^{(4)}(0) = -4 \rightarrow$$

$$f^{(4)}(c) : -4e^c \cdot \cos(c)$$

$$f^{(5)}(x) : -4e^x \cdot \cos(x) + 4e^x \cdot \sin(x) \rightarrow f^{(5)}(0) = -4e^0 \cdot \cos(0) + 4e^0 \cdot \sin(0) = -4 \rightarrow$$

$$f^{(5)}(c) : -4e^c \cdot \cos(c) + 4e^c \cdot \sin(c)$$

sehingga deret Maclaurin $\rightarrow e^x \cdot \cos(x) = 1 + \frac{1}{1!}x + \frac{0}{2!}x^2 - \frac{2}{3!}x^3 - \frac{4}{4!}x^4 - \frac{4}{5!}x^5 + \dots$

$$e^x \cdot \cos(x) = 1 + x + -\frac{2}{3!}x^3 - \frac{4}{4!}x^4 - \frac{4}{5!}x^5 + \dots$$

Deret Taylor

$$e^c \cdot \cos(c) + \frac{e^c \cdot \cos(c) - e^c \cdot \sin(c)}{1!} (x-c) - \frac{2e^c \cdot \sin(c)}{2!} (x-c)^2 - \frac{2e^c \cdot \sin(c) + 2e^c \cdot \cos(c)}{3!} (x-c)^3$$

$$\frac{4e^c \cdot \cos(c)}{4!} (x-c)^4 + \frac{4e^c \cdot \cos(c) - 4e^c \cdot \sin(c)}{5!} (x-c)^5$$

① Deret Taylor dan Maclouren

a. - Deret maclouren

$$\begin{aligned}
 f(x) &= \frac{1}{1+x} \text{ atau } f(x) = (1+x)^{-1} \rightarrow \text{misal } u=1; u'=0 \\
 f'(x) &= 0(1+x)^{-1} + 1(-)(1+x)^{-2} \quad u=(1+x)^{-1} \\
 &= 0 + (-)(1+x)^{-2} \quad v' = -(1+x)^{-2} \\
 &= -(1+x)^{-2} \rightarrow f'(0) = -1 \\
 f''(x) &= 2(1+x)^{-3} \rightarrow f''(0) = 2 \\
 f'''(x) &= -6(1+x)^{-4} \rightarrow f'''(0) = -6
 \end{aligned}$$

$$\begin{aligned}
 \text{Sehingga } f(0) &= 1 - x + \frac{2}{2!} x^2 - \frac{6}{3!} x^3 + \dots \\
 &= 1 - x + \frac{2}{2} x^2 - \frac{6}{6} x^3 + \dots \\
 &= 1 - x + x^2 - x^3 + \dots
 \end{aligned}$$

② a) Deret maclouren

$$\begin{aligned}
 -f(x) &= \sin x \\
 &= \sin 0 + \frac{\cos 0}{1!} x + \frac{-\sin 0}{2!} x^2 + \frac{-\cos 0}{3!} x^3 + \frac{\sin 0}{4!} x^4 + \dots \\
 &= 0 + x - 0 - \frac{x^3}{3!} + 0 + \dots \\
 &= x - \frac{x^3}{3!} + \dots
 \end{aligned}$$

$$\begin{aligned}
 -f(x) &= \cos x \\
 &= \cos 0 + \frac{-\sin 0}{1!} x + \frac{-\cos 0}{2!} x^2 + \frac{\sin 0}{3!} x^3 + \frac{\cos 0}{4!} x^4 + \dots \\
 &= 1 + 0 - \frac{x^2}{2!} + 0 + \frac{x^4}{4!} + \dots \\
 &= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \dots
 \end{aligned}$$

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① DERET TAYLOR:

$$f(x) = \frac{1}{1+x}$$

$$f(0) = \frac{1}{1+0}$$

$$= 1 //$$

$$f(x) = \ln(1+x)$$

$$f(0) = \ln(1+0) //$$

DERET TAYLOR

Contoh: $f(x) = \cos x$

$$\cos(x) = \cos(a) - \frac{\sin(a)}{1!} (x-a) - \frac{\cos(a)}{2!} (x-a)^2 +$$

$$\frac{\sin(a)}{3!} (x-a)^3 + \dots$$

$$\cos(x) = 1 - \frac{0}{1!} (x-0) - \frac{1}{2!} (x-0)^2 + \frac{0}{3!} (x-0)^3 +$$

$$\frac{1}{4!} (x-0)^4 + \dots$$

$$\cos(x) = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \dots$$

Contoh: $f(x) = \sin x$

$$= f(a) + f'(a)(x-a) + \frac{f''(a)}{2!} (x-a)^2 +$$

$$\frac{f^{(3)}(a)}{3!} (x-a)^3 + \dots + \frac{f^{(n)}(a)}{n!} (x-a)^n + \dots$$

$$\frac{1}{1-x} = \frac{1}{1-a} + \frac{x-a}{(1-a)^2} + \frac{(x-a)^2}{(1-a)^3} + \dots$$

$$\cos x = \cos a - \sin a (x-a) - \frac{1}{2} \cos a (x-a)^2 + \frac{1}{6} \sin a (x-a)^3 + \dots$$

$$e^x = e^a \left[1 + (x-a) + \frac{1}{2} (x-a)^2 + \frac{1}{6} (x-a)^3 + \dots \right]$$

$$\ln x = \ln a + \frac{x-a}{a} - \frac{(x-a)^2}{2a^2} + \frac{(x-a)^3}{3a^3} - \dots$$

$$\sin x = \sin a + \cos a (x-a) - \frac{1}{2} \sin a (x-a)^2 - \frac{1}{6} \cos a (x-a)^3 + \dots$$

DERET MA CL LOREN :

$$f(x) = \sin x$$

$$f'(x) = \cos x$$

$$f''(x) = -\sin x$$

$$f'''(x) = -\cos x$$

$$f^{(4)}(x) = \sin x \text{ dst.}$$

jaras

$$\sin x = \sin 0 + \frac{\cos 0}{1!} x + \frac{-\sin 0}{2!} x^2 + \frac{-\cos 0}{3!} x^3 + \frac{\sin 0}{4!} x^4 + \dots$$

$$= 0 + x - 0 - \frac{x^3}{3!} + 0 + \dots$$

$$= x - \frac{x^3}{3!} + \dots$$

DENGAN CARA YANG SAMA.

$$\cos x = \cos 0 + \frac{-\sin 0}{1!} x + \frac{-\cos 0}{2!} x^2 + \frac{\sin 0}{3!} x^3 - \frac{\cos 0}{4!} x^4 + \dots$$

$$= 1 + 0 - \frac{x^2}{2!} + 0 + \frac{x^4}{4!} + \dots$$

$$= 1 - \frac{x^2}{2!} + \frac{x^4}{4!} + \dots$$

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