

## Extracted Social Network Mining

Mahyuddin K. M. Nasution

Fakultas Ilmu Komputer dan Teknologi Informasi (Fasilkom-TI)  
Universitas Sumatera Utara, Padang Bulan, Medan 20155, Sumatera Utara, Indonesia  
e-mail: mahyuddin@usu.ac.id, nasutionmahyu2012@gmail.com

### *Abstract*

*In this paper we study the relationship between the resources of social networks by exploring the Web as big data based on a simple search engine. We have used set theory by utilizing the occurrence and co-occurrence for defining the singleton or doubleton spaces of event in a search engine model, and then provided them as representation of social actors and their relationship in clusters. Thus, there are behaviors of social actors and their relation based on Web.*

**Keywords :** *Singleton, doubleton, cluster, behavior*

## 1 INTRODUCTION

An extracted social network is a resultant from the methods of extracting social network from information sources (web pages, documents, or corpus) [1] or the transformation of the raw data into a social network (pre-processing) [2]. However, Web not only dealing with everything changed dynamically [3], but Web as social media represent all members of social (population) [4, 5], or containing big data as big picture of world. Thus, extraction of social networks always based on parts of social (communities) [6], and then to analyze it so that enable to generate useful information, for example, in the decision making [7]. This needs the sample that can represent population. Therefore, for getting significance of information source and trust, in the extracted social networks need the suitable approaches [8].

In other side, the resources of social network such as vertices/actors, edges/relations, and Web/documents have the relations between one to another [9]. A lot of relations between vertices and edges for expressing some of social structures in Social Network Analysis (SNA) [10], but still a little formula to get information about relations among first two resources and Web [11]. Therefore, this needs a formalism study about resources. In all sides of social network, this paper aimed to provide a basic means of discovering knowledge formally about the extracted social network, we call it social network mining.

## 2 RELATED WORK AND MOTIVATION

The social networks can be modeled naturally by the graph  $G < V, E >$  where  $V = \{v_i | i = 1, \dots, n\}$  is a set of vertices, and  $\{e_j | j = 1, \dots, m\}$  is a set of edges and  $e_j$  in  $E$  if two

vertices  $vk$  in  $V$  and  $vl$  in  $V$  are adjacent, or  $e_j = v_kv_l = v_lv_k$  [12]. In pre-processing of social network mining, extracting the social network from the information sources is the relatively approaches which is formed through modal relations [1]. One of extraction methods is the superficial method that depends heavily on the occurrence and the co-occurrence [3].

Let a word "Web" or a phrase "World Wide Web" is representation an object according to what we think [13]: the computer network is a social network [14]. In expressing the behavior of social, Natural language processing (NLP) as basic layer of social network mining, and we define the term related it as follows.

*Definition 1.* A term  $t_x$  consists of at least one or a set of words in a pattern, or  $t_x = (w_1, \dots, w_l), l \leq k, k$  is a number of words  $w(s), l$  is number of vocabularies (tokens) in  $t_x, |t_x| = k$  is size of  $t_x$ .

In NLP, 'Shahrul Azman Noah' and 'Opim Salim Sitompul' as terms, for example, are well-defined names of social actor. We have defined a dynamic space based on concept of NLP application as follows [15].

*Definition 2.* Let a set of web pages indexed by search engine by  $\Omega$ . For each search term  $t_x$ , where  $t_x$  in  $\sum$ , i.e. a set of singleton search term of search engine. There are a dynamic space  $\Omega$  containing the ordered pair of the term  $t_{xi}i = 1, \dots, I$  and web pages  $\omega_{xj}j = 1, \dots, J : (t_{xi}, \omega_{xj}) = (t_x, \omega_x)_{ij}$ , or a vector space  $\Omega_x = (t_x, \omega_x)_{ij}$  (is subset of or equal to  $\Omega$ ) is a singleton search engine event of web pages (singleton event) that contain an occurrence (event) of  $t_x$  in  $\omega$ .

*Definition 3.* Suppose  $t_x$  in  $q$  and  $q$  is a query. Clustering web pages based on query is an implication, i.e if  $\omega \rightarrow t_x$  is TRUE then a web page  $\omega$  in  $\Omega$  is relevant to  $q$  or  $\Omega_x = 1$  if  $t_x$  is true at all  $\omega$  in  $\Omega$ , 0 otherwise, and  $\Omega_x$  as the cluster of  $t_x$ .

Classically, a logical implication associated with inference [16].

Lemma 1. If  $|\Omega|$  is the cardinality of  $\Omega$  and  $|\Omega_x| \leq |\Omega|$  then probability of a singleton event  $\Omega_x$  is

$$P(t_x) = |\Omega_x|/|\Omega| \text{ in } [0, 1]$$

*Proof.* For any term  $t_x$  in  $q$ , each web page  $\omega$  in  $\Omega$  is relevant to a query  $q$  has a probability to other web pages in  $\Omega, 0 \leq p(\omega) = 1/|\Omega| \leq 1$ . Probability of all web pages that relevant to a query in  $\Omega$  is  $0 \leq p(\Omega_x) = \sum p(\omega) = |\Omega_x|/|\Omega| \leq 1$ , or  $P(t_x) = p(\Omega_x)$ .

In the same concept we have to define also the co-occurrence based on NLP [17].

*Definition 4.* Let  $t_x$  and  $t_y$  are two different search terms,  $t_x \neq t_y, t_x, t_y$  in  $\sum$ , where  $\sum$  is a set of singleton term of search engine. There are a dynamic space  $\Omega$  containing the ordered pair of two terms  $\{t_{xi}, t_{yi}\}i = 1, \dots, I$  and web pages  $\omega_{xj}j = 1, \dots, J : (\{t_{xi}, t_{yi}\}, \omega_{xyj}) = (\{t_x, t_y\}, \omega_{xy})_{ij}$ , or a vector space  $\Omega_x \cap \Omega_y = (\{t_x, t_y\}, \omega_{xy})_{ij}$  (is a subset of or equal to  $\Omega$ ) is a doubleton search engine event of web pages (doubleton event) that contain a co-occurrence (event) of  $t_x, t_y$  in  $\omega$ .

*Lemma 2.* If  $|\Omega|$  is the cardinality of  $\Omega$  and  $|\Omega_x \cap \Omega_y| \leq |\Omega|$  then probability of a doubleton event  $\Omega_x \cap \Omega_y$  is

$$P(\{t_x, t_y\}) = |\Omega_x \cap \Omega_y|/|\Omega| \text{ in } [0, 1]$$

*Proof.* As direct consequence of: Definition 4 and Lemma 1.

At the time conducting the extraction for getting occurrences and co-occurrence, we submitted the queries containing the name to Google search engine, we have the hit count = 20,000 for 'Shahrul Azman Noah' (as occurrence) and = 3,000 for 'Opim Salim Sitompul'

(as occurrence), while the hit count for 'Shahrul Azman Noah,Opim Salim Sitompul' (as co-occurrence) is 218. However, if the query contains names that are enclosed in quotation marks, produced the hit count = 2,680 for "Shahrul Azman Noah" (as occurrence) and the hit count = 5,650 for "Opim Salim Sitompul" (as occurrence), while the hit count for ""Shahrul Azman Noah", "Opim Salim Sitompul"" (as co-occurrence) is 61. Therefore, information about social actors in occurrence and social networks in co-occurrences are different in behavior, and we have an assumption [18, 19]: Each probability of forming its own distribution. Different data distribution gives different behavior. In this case, we have the problem.

*Theorem 1.* The behavior of clusters describes the behavior of a social actor, then the behavior of other actors expressed by the relationships between the clusters.

### 3 MODEL AND APPROACH

Literally, we can identify social actor based on Named-Entity Recognition (NER) in web pages or any document as follow.

*Definition 5.* Suppose there are the well-defined actors, then there is  $A = \{\alpha_i | i = 1, \dots, n\}$  as a set of social actors.

Each actor literally also has attributes, thus we can define it as follow [20].

*Definition 6.* Suppose there be the well-identified attributes, then there is  $B = \{b_j | j = 1, \dots, m\}$  as a set of attributes of actors.

*Definition 7.* For all pairs (dyads) of  $n$  social actors, a set of relationships  $R = \{r_p | p = 1, \dots, m\}$  where a relationship between two actors there are a tie connect them by one or more relations, or  $r_p(\alpha_k, \alpha_l) = B_{\alpha_k} \cap B_{\alpha_l}$ .

*Definition 8.* An extracted social network, i.e.  $SN = \langle V, E, A, R, \gamma_1, \gamma_2 \rangle$  satisfies the conditions as follow:

1.  $\gamma_1(1 : 1)A \rightarrow V$ , and
2.  $\gamma_2 : R \rightarrow E$

As an approach to formalize the relationship between resources of social networks, and for exploring the behavior, we use the association rule.

*Definition 9.* Let  $B = \{b_1, b_2, \dots, b_m\}$  is a set of attributes. Let  $M_i$  is a set of transactions are subsets of attributes or  $M_i$  are the subset of or equal to  $B$ . The implication  $\Omega_{bk} \rightarrow \Omega_{bl}$  with two possible value TRUE or FALSE as an *association rule* if  $\Omega_{bk}, \Omega_{bl}$  are subset of  $B$  and  $\Omega_{bk} \cap \Omega_{bl} = \phi$ .

### 4 FORMULATION OF BEHAVIOR

Each cluster represents an actor based on the extraction of social networks.

*Lemma 3.* If for a cluster  $\Omega_x$  of a search term  $t_x$  there exist other cluster  $\Omega_y$  of a search term  $t_y$  where  $t_x \neq t_y$ , then  $\Omega_x$  is a stand-alone cluster.

*Proof.* Based on *Definition 2* and *Definition 9*, we have  $t_x \rightarrow t_y$  literally or  $\Omega_x \rightarrow \Omega_y$ , but  $t_x \neq t_y$  such that  $\Omega_x \cap \Omega_y = \square$ . Therefore,  $\Omega_x$  is a stand-alone cluster.

*Proposition 1.* If  $t_{\alpha_i}$  in  $qi = 1, \dots, n$  and  $\Omega_{\alpha_i}$  are a stand-alone cluster for each of  $\{\alpha_1, \alpha_2, \dots, \alpha_n\} = A$ , then  $\Omega_{\alpha_i}$  represent the behavior of  $\alpha_i$  in  $A$ , respectively.

*Proof.* Based on *Definition 9*, we have  $\omega$  in  $\Omega \rightarrow t_{\alpha}$  in  $q$  and  $\omega$  is representation of actor  $\alpha$  in  $A$ , and because of each  $\omega$  in  $\Omega$  has a probability then  $\omega$  in  $\Omega$  be the behavior of actor

$\alpha$  in  $A$ , but based on *Definition 2*  $\Omega\alpha = \{(t_a, \omega_a)_{ij}\}$ ,  $\Omega_a$  is representation of  $\alpha$  in  $A$ . Let there be  $t_{ak}, t_{al}$  in  $qt_{ak} \neq t_{al}$ , we have  $\Omega_{ak} \rightarrow \Omega$  and  $\Omega_{al} \rightarrow \Omega$ : Even though  $\Omega_{ak} \rightarrow \Omega_{al}$  or  $\Omega_{al} \rightarrow \Omega_{ak}$ , but  $\Omega_{ak} \cap \Omega_{al} = \Omega_{al} \cap \Omega_{ak} = \phi$ . Each of  $\Omega_{\alpha i}, i = 1, \dots, n$  is a stand-alone cluster that represent the behavior of an actor.

*Lemma 4.* Let  $t_{ak} \neq t_{al}$  is the different search terms represent two social actors. If  $t_{ak}, t_{al}$  in  $q$ , then  $\Omega_{akl}$  is a stand-alone cluster for a pair of social actors.

*Proof.* As applicable in *Lemma 3* to *Definition 3* and *Definition 2*,  $\omega$  in  $\Omega \rightarrow \{t_{ak}, t_{al}\}$  in  $q$  or  $\omega$  in  $\Omega \rightarrow \{t_{ak} \square t_{al}\}$  in  $q$  and  $(\omega$  in  $\Omega \rightarrow t_{ak}$  in  $q) \square (\omega$  in  $\Omega \rightarrow t_{al}$  in  $q)$  and we have  $\Omega_{ak} \rightarrow \Omega_{al}$  and  $t_{ak} \neq t_{al}$ , but  $\Omega_{ak} \cap \Omega_{al} \neq \phi$  then  $\Omega_{al} \rightarrow \Omega_{ak}$ . However, based on *Definition 9* we have  $((\Omega_{ak} \rightarrow \Omega_{al}) \rightarrow \Omega) = ((\Omega_{al} \rightarrow \Omega_{ak}) \rightarrow \Omega)$ . In other word,  $\Omega_{akl} = \{(t_{akl}, \omega_{akl})_{ij}\} = \{(t_{ak} \square t_{al}, \omega_{ak} \square \omega_{al})_{ij}\} = \{(t_a \square t_a, \omega_a \square \omega_a)_{ij}\} (i, j = k \square l) = \{(t_a, \omega_a)_{ij}\} (i, j = k \square l) = \Omega_a$ . Thus,  $akl$  is a stand-alone cluster of a pair of social actors.

*Proposition 2.* If  $\Omega_{akl}$  is a stand-alone cluster for a pair of  $\{a_1, a_2, \dots, a_n\} = A$ , then  $\Omega_{akl}$  represent the behavior of relationship between  $a) i$  in  $A, i = 1, \dots, n$ .

*Proof.* Based on *Lemma 4* we have  $\Omega_{akl} = \Omega_a$ , and  $\Omega_a = \{(t_a, \omega_a)_{ij}\} = \{(t_a \square t_a, \omega_a \square \omega_a)_{ij}\} = \{(t_{ak} \square t_{al}, \omega_{ak} \square \omega_{al})_{ij}\} (i, j = kl) = \{(t_{ak} \square t_{al}, \omega_{ak} \square \omega_{al})\} = \{(t_{ak}, \omega_{ak}) \square (t_{al}, \omega_{al})\} = \{(t_{ak}, \omega_{ak})\} \cap \{(t_{al}, \omega_{al})\} = \Omega_{ak} \cap \Omega_{al}$ . Or because name also can be an attribute of social actor, then Based on *Definition 7* we have  $\Omega_{ak} \cap \Omega_{al} = B_{ak} \cap B_{al} = r_p(a_k, a_l)$ .

*Definition 8* has set the existence of a social actor by means of  $\gamma_1$  and behavior of a social actor based on the result clusters (*Proposition 1*, while the behavior of relationship between social actors refers to the cluster based on dyad (*Proposition 2*) and this behavior based on  $\gamma_2$  also become behavior of an edge in social network. Specially, in superficial methods  $r_p$  in  $R$  means the strength relation between two actors  $ak$  and  $al$  in  $A$  by involving one or more of the similarity measurements: mutual information, Dice coefficient, overlap coefficient, cosine, or for example Jaccard coefficient

$$J_c = |\Omega_{ak} \cap \Omega_{al}| / (|\Omega_{ak}| + |\Omega_{al}| - |\Omega_{ak} \cap \Omega_{al}|) \text{ in } [0, 1]$$

In this concept of similarity,  $B)ak \cap B_{al} = |\Omega_{ak} \cap \Omega_{al}| / (|\Omega_{ak}| + |\Omega_{al}| - |\Omega_{ak} \cap \Omega_{al}|) = J_c$  such that  $e_j$  in  $E$  if  $r_p > 0$ . However the behavior of  $r_p (0 \leq r_p \leq 1)$  depends on the behavior of  $\Omega_{ak}$  is a subset of  $\Omega$ ,  $\Omega_{al}$  is subset of  $\Omega$  and  $\Omega_{ak} \cap \Omega_{al}$  is a subset of  $\Omega$ :  $|\Omega_{ak}| \leq |\Omega_{al}|$  or  $|\Omega_{ak}| \geq |\Omega_{al}|$ ,  $|\Omega_{ak} \cap \Omega_{al}| \leq |\Omega_{ak}|$ , and  $|\Omega_{ak} \cap \Omega_{al}| \leq |\Omega_{al}|$ . If another measurement concept is similar to  $J_c$ , then *Theorem 1* is proved. Therefore, we have

*Corollary 1.* If the behavior of social actors behaves in clusters (of big data) then the behavior of the clusters (of big data) can be represented by the extracted social network.

## 5 CONCLUSIONS

In this social network study we have presented an analysis for formulating the behavior of resources of social network as a social network mining. Formulation based on a search engine model and the clustering model, and we have obtained an explanation that there are relations between social actors/vertices, relationships/edges, and documents/web based on the clusters are formed. The future work will involve the extraction of a social network to describe the research collaboration for exploring the behavior of social actors and their relationships.

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